

Minimal-Precision Computing for High-Performance, Energy-Efficient, and Reliable Computations

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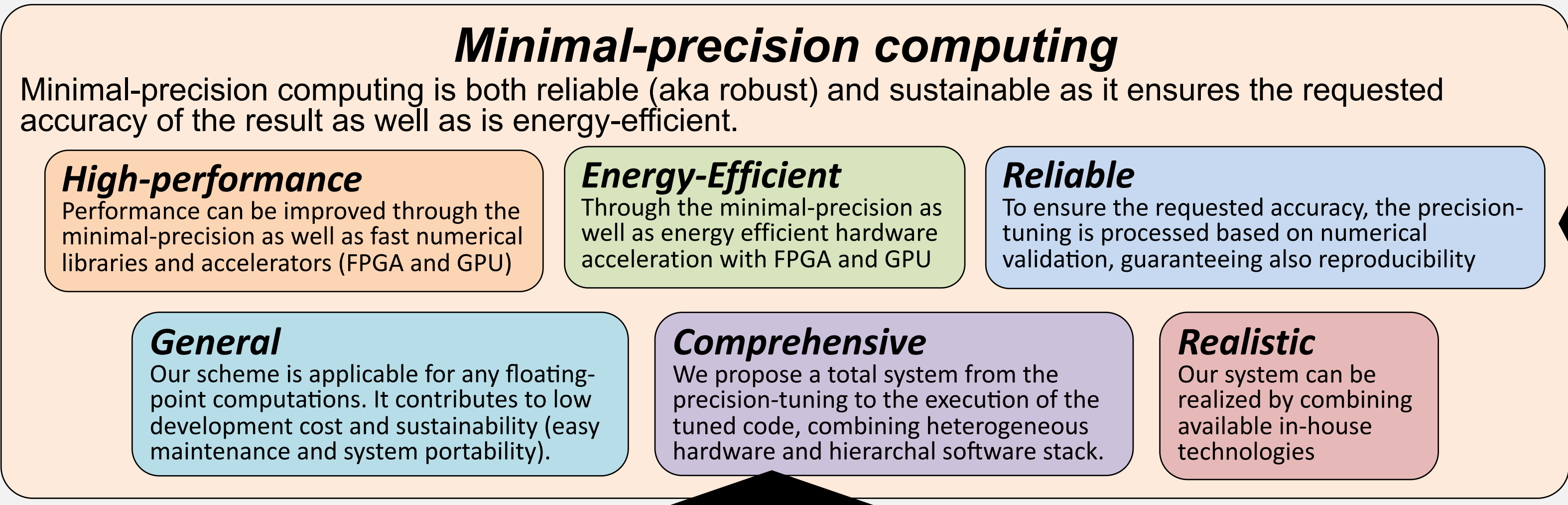
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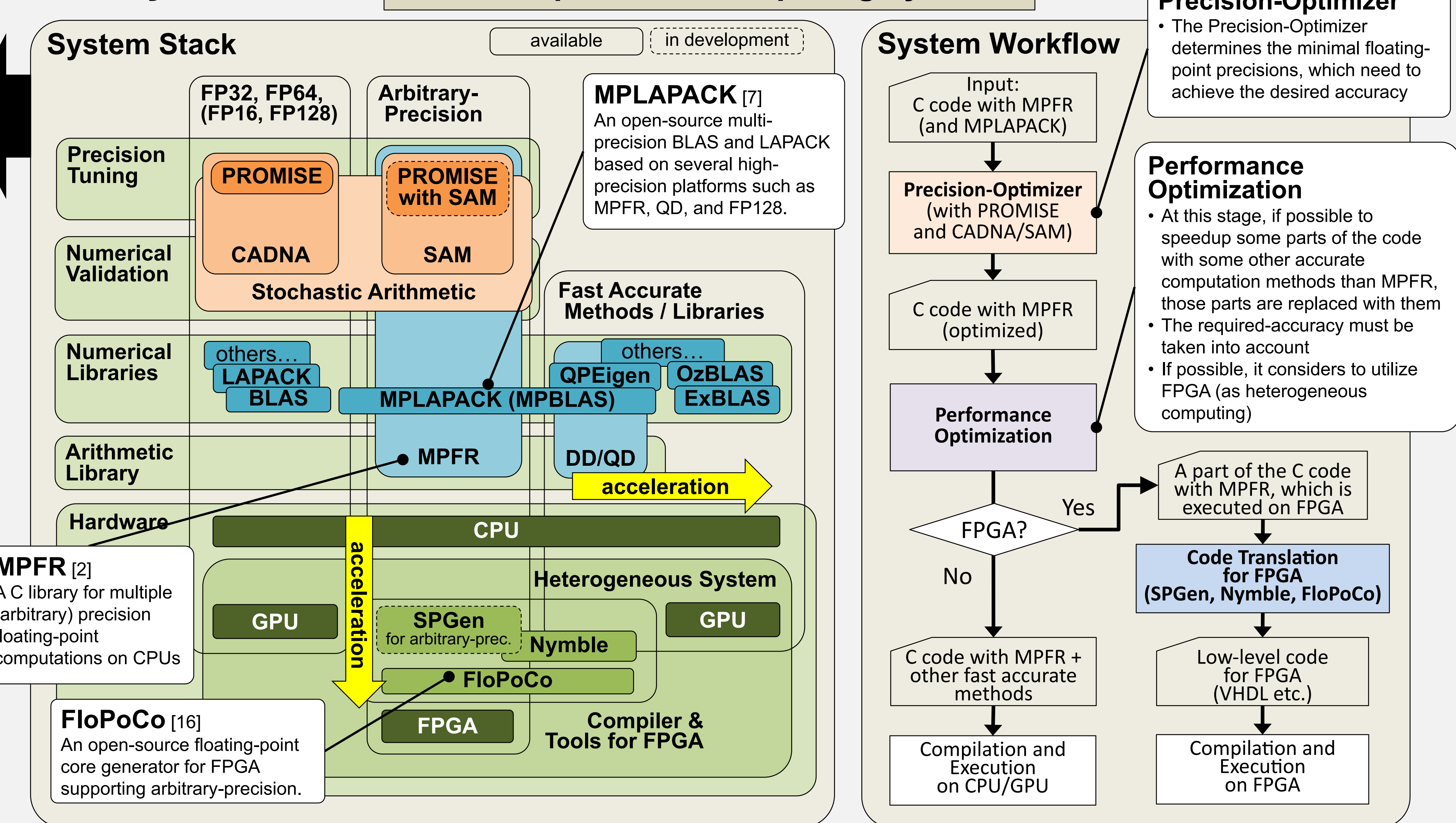
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Introduction

In numerical computations, the precision of floating-point computations is a key factor to determine the performance (speed and energy-efficiency) as well as the reliability (accuracy and reproducibility). However, the precision generally plays a contrary role for both. Therefore, the ultimate concept for maximizing both at the same time is the minimal-precision computation through precision-tuning, which adjusts the optimal precision for each operation and data. Several studies have been already conducted for it so far, but the scope of those studies is limited to the precision-tuning alone. In this study, we propose a more broad concept of the minimal-precision computing with precision-tuning, involving both hardware and software stack.



Our System



(1) Precision-tuning with numerical validation based on stochastic arithmetic

Rounding-errors can be estimated stochastically with a reasonable cost (for details, see "A. Stochastic Arithmetic Tools" at the bottom left). General scheme applicable for any floating-point computations

Tools:

- PROMISE [17]** (based on a stochastic arithmetic library, CADNA [18]), Verrou [19], etc.

Issues on existing studies:

- Some existing methods (e.g., Precimonious [20], GPUMixer [22]) are not based on any verification / validation
- No adaptation for heterogeneous systems with FPGA
- The other validation / verification methods:
 - Theoretical error analyses: classic approach based on theory, but not general (analysis is needed for each numerical method) and not easy if the code is huge and complex
 - Interval computations provides guaranteed, but may be over-estimated bounds, or a special algorithm is needed for each numerical method, not well suited for large codes

(2) Arbitrary-precision libraries and fast accurate numerical libraries

Reduced-/mixed-precision with FP16/FP32/FP64 enables us to improve performance & energy-efficiency. High-precision libraries and fast accurate computation methods have been developed for reliable & reproducible computation

Tools:

- High-precision arithmetic: binary128 (intel, gcc), QD [1], MPFR [2], ARPREC [3], CAMPARY [4], etc.
- Accurate sum/dot: AccSum/Dot [5], Ozaki-scheme [6], etc.
- Numerical libraries: MPLAPACK [7], QPEigen [8], QPBLAS [9], XBLAS [10], ReprBLAS [11], ExBLAS [12], OzBLAS [13], etc.

Issues on existing studies:

- Lack of precision-tuning method
- Correct-rounding may be over-accurate and slow
- Numerical verification or validation may be more important than bit-level reproducibility

(3) Field-Programmable Gate Array (FPGA) with High-Level Synthesis (HLS)

FPGA enables us to implement any operations on hardware, including arbitrary-precision operations. HLS enables us to use FPGAs through existing programming languages such as C/C++ and OpenCL. FPGA can be used to perform arbitrary-precision computations on hardware efficiently (high-performance and energy-efficient)

Tools:

- Compilers: SPGen [14], Nymble [15], etc.
- Custom floating-point operation generator: FloPoCo [16], etc.

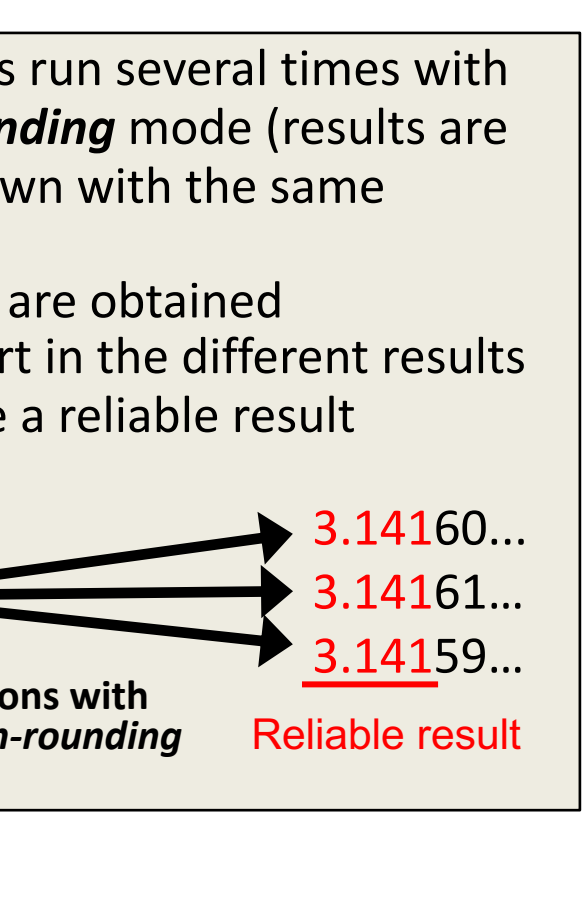
Issues on existing studies:

- Lack of precision-tuning method
- Adaptation for HPC as a heterogeneous platform is still at new stage

Our Contributions

A Stochastic Arithmetic Tools

Discrete Stochastic Arithmetic (DSA) [21] enables us to estimate rounding errors (i.e., the number of correct digits in the result) with 95% accuracy by executing the code 3 times with random-rounding. DSA is a general scheme applicable for any floating-point operations: no special algorithms and no code modification are needed. It is a light-weight approach in terms of performance, usability, and development cost compared to the other numerical verification / validation methods.



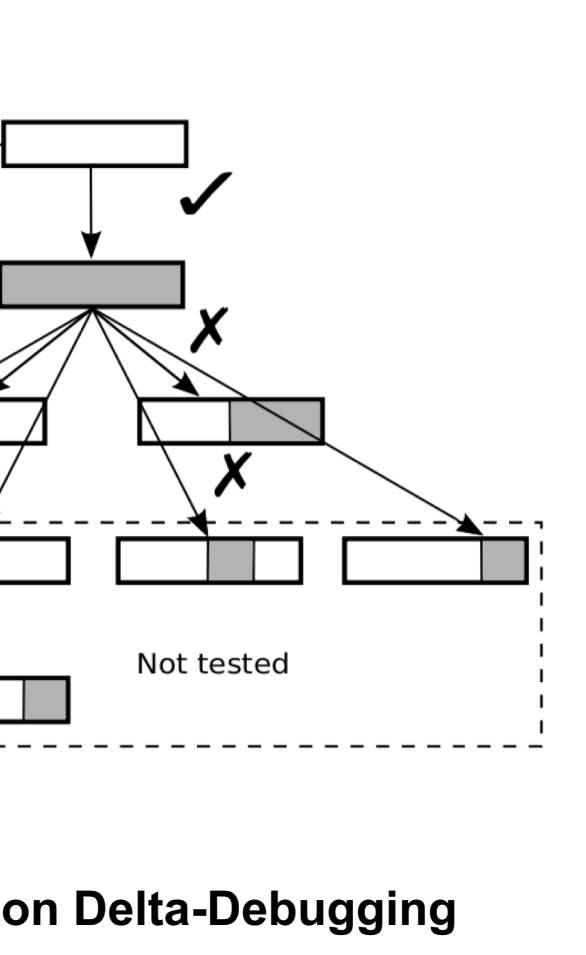
CADNA & SAM (Sorbonne University)

CADNA (Control of Accuracy and Debugging for Numerical Applications) [18] is a DSA library for FP16/32/64/128. CADNA can be used on CPUs in Fortran/C/C++ codes with OpenMP & MPI and on GPUs with CUDA. SAM (Stochastic Arithmetic in Multiprecision) [23] is a DSA library for arbitrary-precision with MPFR.



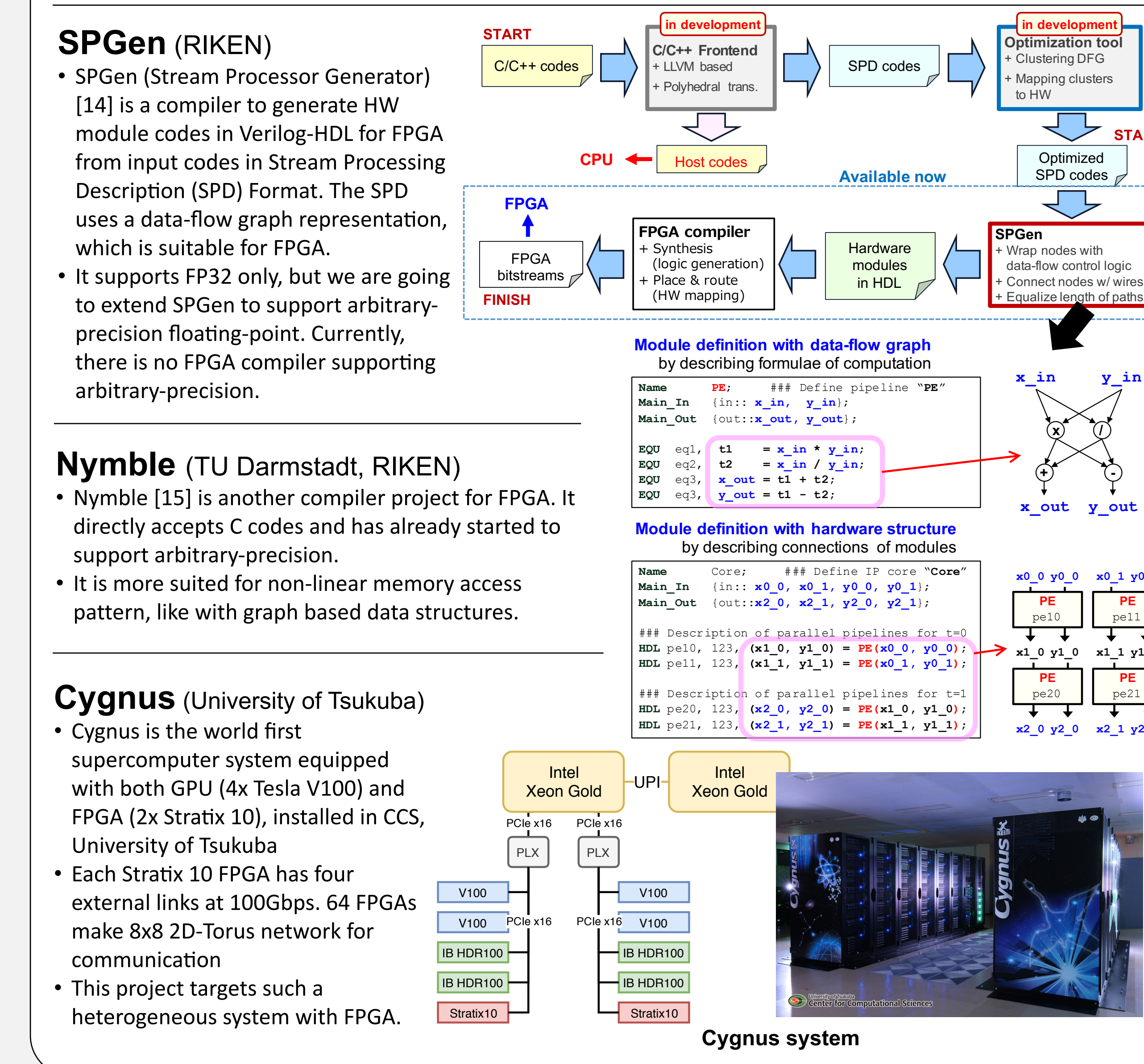
PROMISE (Sorbonne University)

PROMISE (PRecision OptiMISE) [17] is a tool based on Delta-Tuning [24] to automatically tune the precision of floating-point variables in C/C++ codes. The validity of the results is checked with CADNA. We are going to extend PROMISE for arbitrary-precision with MPFR



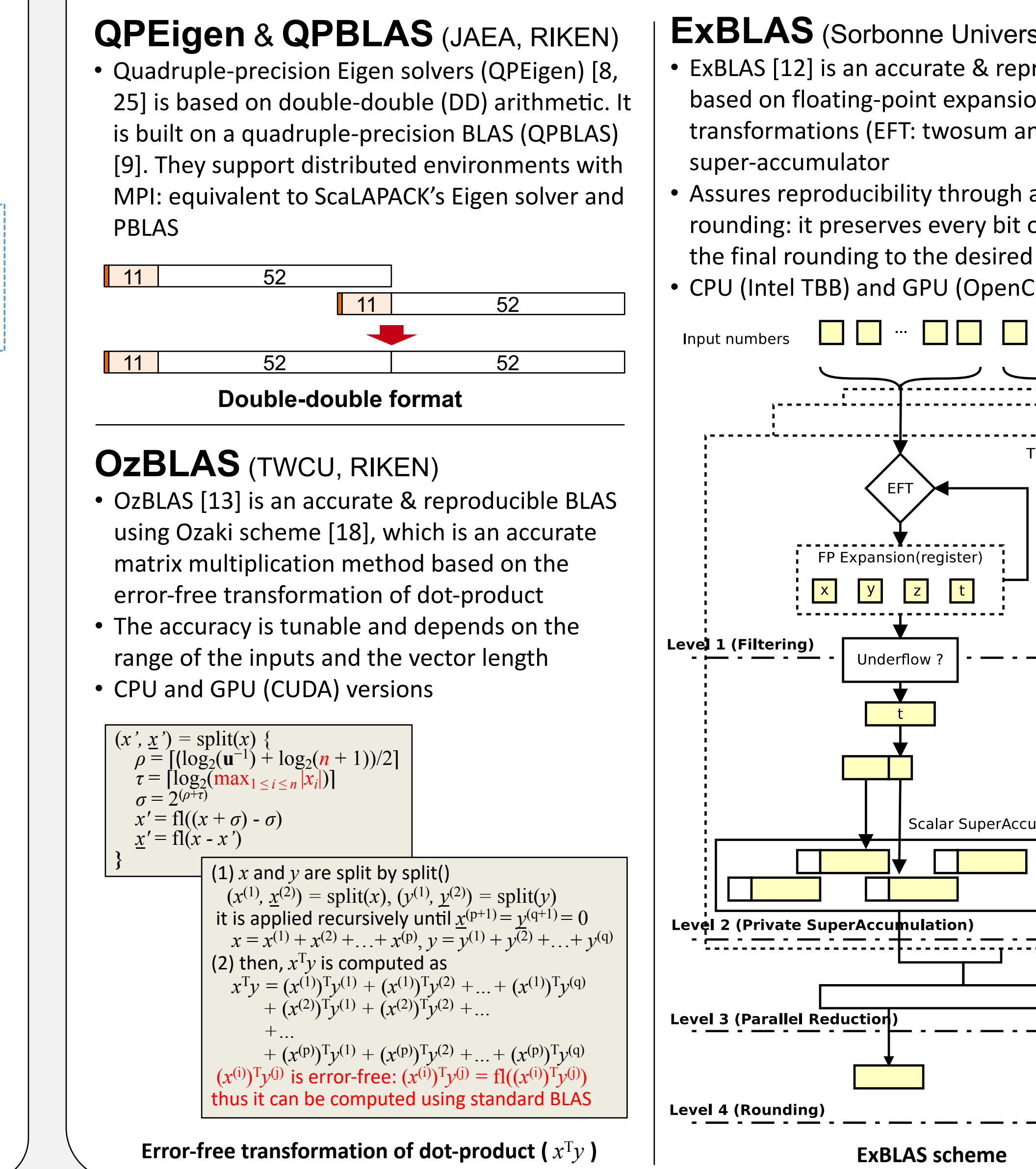
B FPGA as an Arbitrary-Precision Computing Platform

FPGA enables us to implement arbitrary-precision on hardware. High-Level Synthesis (HLS) enables us to program it in OpenCL. However, compiling arbitrary-precision code and obtaining high performance are still challenging. Heterogeneous computing with FPGA & CPU/GPU is also a challenge



C Fast and Accurate Numerical Libraries

Arbitrary-precision arithmetic is performed using MPFR on CPUs, but the performance is very low. To accelerate it, we are developing several numerical libraries supporting accurate computation based on high-precision arithmetic or algorithmic approach. Some software also support GPU acceleration.



Conclusion & Future Work

We proposed a new systematic approach for minimal-precision computations. This approach is reliable, general, comprehensive, high-performance, and realistic. Although the proposed system is still in development, it can be constructed by combining already available (developed) in-house technologies as well as extending them. Our ongoing step is to demonstrate the system on a small application.

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